

Homework 4

Phys 1140, Fall 2012

Prof. Markus B. Raschke

Due: Tuesday, **October 9**, 4 pm, in your TA's hw box in G2B66

This is your last homework assignment!

1) (7 points) We want to revisit a problem on error propagation similar to one we had on an earlier hw, but analyze it in a little more depth. We want to calculate $z = x \cos^2(\Theta)$, and understand for which values of Θ we are more or less sensitive to the uncertainty of Θ .

- Take $x = 1.203 \pm 0.002$ meters, $\Theta = (45.5 \pm 0.5)$ degrees. Calculate $z \pm \delta z$.
- Repeat the calculation with $x = 1.203 \pm 0.002$ meters, $\Theta = (5.5 \pm 0.5)$ degrees.
- Discuss why δz is different for both cases, despite identical uncertainties in x and Θ ? Use a suitable graph to illustrate your explanation.

2) (7 points) The period of a pendulum is measured by six students, and they report their values as 2.51, 2.48, 2.51, 2.52, 2.45, and 2.53 seconds, respectively.

- What is the average value for the period, T , and the statistical uncertainty (standard error on the mean) for T ? State your final answer for $T_{\text{avg}} \pm \delta T$ with proper sig figs.
- The students want a statistical uncertainty that is half of what is calculated above. How many total number of measurements will they need to make (including the 6 above), assuming that the spread in their measurements (s) remains the same? State your reasoning in words.

3) (6 points) You measure a velocity of some particles many thousands of times, and find that the average is 90.7 m/s, and that the standard deviation on an individual measurement is 2 m/s. Now, you take an additional 20 measurements, and take the average just of those 20 measurements. What is the probability that you find that average to be either greater than 91.6 m/s, or less than 89.8 m/s?